Practice by Example

Is each equation a direct variation? If it is, find the constant of variation.

Example 1

1.
$$2y = 5x + 1$$

2.
$$8x + 9y = 10$$

3.
$$-12x = 6y$$

4.
$$y + 8 = -x$$

$$5.5x - 6y = 0$$

6.
$$-4 + 7x + 4 = 3y$$

7.
$$-x = 10y$$

8.
$$0.7x - 1.4y = 0$$

$$9. \ \frac{1}{2}x + \frac{1}{3}y = 0$$

Example 2 (page 262)

Write an equation of the direct variation that includes the given point.

13.
$$(-5, -9)$$

Chapter 5 Graphs and Functions

Example 3 (page 263) Define the variables. Then write a direct variation to model each relationship.

- 22. Geometry The perimeter of a regular octagon varies directly with the length of one side of the cate. one side of the octagon.
 - 23. Earnings When you have a job that pays an hourly wage, the amount you earn varies directly with the number of hours you work. Suppose you earn \$7.10/hour working at the library.

Example 4 (page 263) For the data in each table, tell whether y varies directly with x. If it does, write an equation for the direct variation.

1				
24.	X	У		
	3	5.4		
	7	12.6		
	12	21.6		

		5 900
5.	Х	y
	-2	1
	3	6
	8	11

6.	X	y
	-6	9
	1	-1.5
	8	-12

Example 5 (page 264)

- 27. Physics The maximum weight you can lift with a lever varies directly with the amount of force you apply. Suppose you can lift a 50-lb weight by applying 20 lb of force to a certain lever.
 - a. What is the ratio of weight to force for the lever?
 - b. Write a proportion and find the force you need to lift a friend weighing 130 lb.
- 28. Bicycling A bicyclist traveled at a constant speed during a timed practice period. Write a proportion to find the distance the cyclist traveled in 30 min.

A Bicyclist's Practices

Abicy		
Elapsed Time	Distance	
10 min	3 mi	
25 min	7.5 mi	

Apply Your Skills

Write an equation of the direct variation that includes the given point.

29.
$$(3, \frac{1}{2})$$

30.
$$\left(\frac{1}{4}, -5\right)$$

31.
$$\left(\frac{-5}{6}, \frac{6}{5}\right)$$

34.
$$\left(-2, \frac{1}{16}\right)$$

36.
$$\left(-\frac{8}{3}, -\frac{9}{8}\right)$$



29. $(3, \frac{1}{2})$ **30.** $(\frac{1}{4}, -5)$ **31.** $(\frac{-5}{6}, \frac{6}{5})$ **32.** (1.2, 7.2) **33.** (0.5, 4.5) **34.** $(-2, \frac{1}{16})$ **35.** (5.2, -1.5) **36.** $(-\frac{8}{3}, -\frac{9}{8})$ 37. a. Writing How can you tell whether two sets of data vary directly? b. How can you tell if a line is the graph of a direct variation?

Critical Thinking Is each statement true or false? Explain.

- 38. The graph of a direct variation may pass through (-2,4).
- 39. The graph of a direct variation may pass through (0,3).
- **40.** If you triple an x-value of a direct variation, the y-value also triples.

Graph the direct variation that includes the given point. Write an equation of the line. **42.** (-2,5) **43.** (2, -5) **44.** (-2, -5)

42.
$$(-2,5)$$

Real-World Connection

You must be at least 17 years old and weigh at least 110 pounds to give blood.

- 45. Biology The amount of blood in a person's body varies directly with body weight. A person who weighs 160 lb has about 5 qt of blood.

 - a. Find the constant of variation. **b.** Write an equation relating quarts of blood to weight.
 - c. Open-Ended Estimate the number of quarts of blood in your body.



- 46. Electricity Ohm's Law $V = I \times R$ relates the voltage, current, and resistant a circuit. V is the voltage measured in volts. I is the current measured in amperes. R is the resistance measured in ohms.
 - a. Find the voltage of a circuit that has a current of 24 amperes and resistant
 - b. Find the resistance of a circuit that has a current of 24 amperes and a volume of 18 volts.



The ordered pairs in each exercise are for the same direct variation. Find each missing value.

48.
$$(-1,2)$$
 and $(4,y)$

49.
$$(-5,3)$$
 and $(x,-4)$

50.
$$(1, y)$$
 and $(\frac{3}{2}, -9)$

51.
$$(2,5)$$
 and $(x,12.5)$

52.
$$(-2,5)$$
 and $(x,-5)$

oblem Solving Hint

Exercise 53, start th the relationship miles and gallons: = 24.



- 💞 53. Gas Mileage A car gets 24 miles per gallon. The number of gallons g of gas used varies directly with the number of miles m traveled.
 - a. Suppose the price of gas is \$1.83 per gallon. Write a function relating the c for g gallons of gas. Is this a direct variation?
 - **b.** Write a direct variation relating the cost of gas to the miles traveled.

Standardized Test Pron